

# The Phase Diagram of Supercooled Water

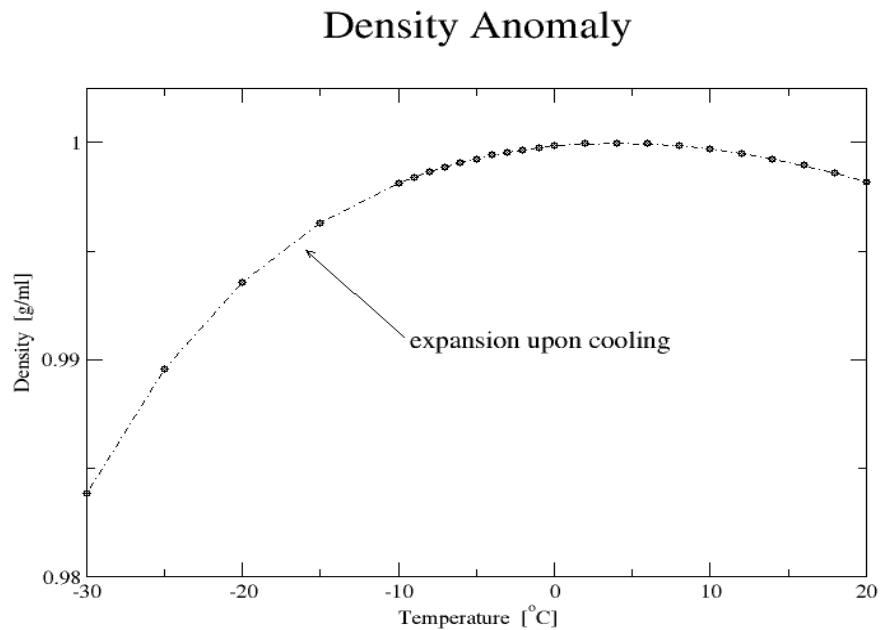
Kevin Stokely

G. Franzese, H. E. Stanley

February 29, 2012  
APS Meeting

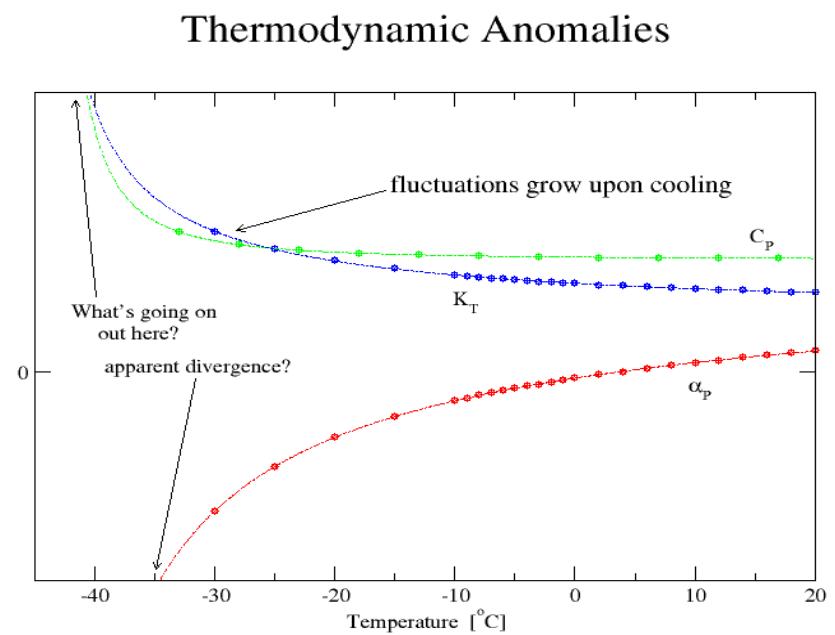
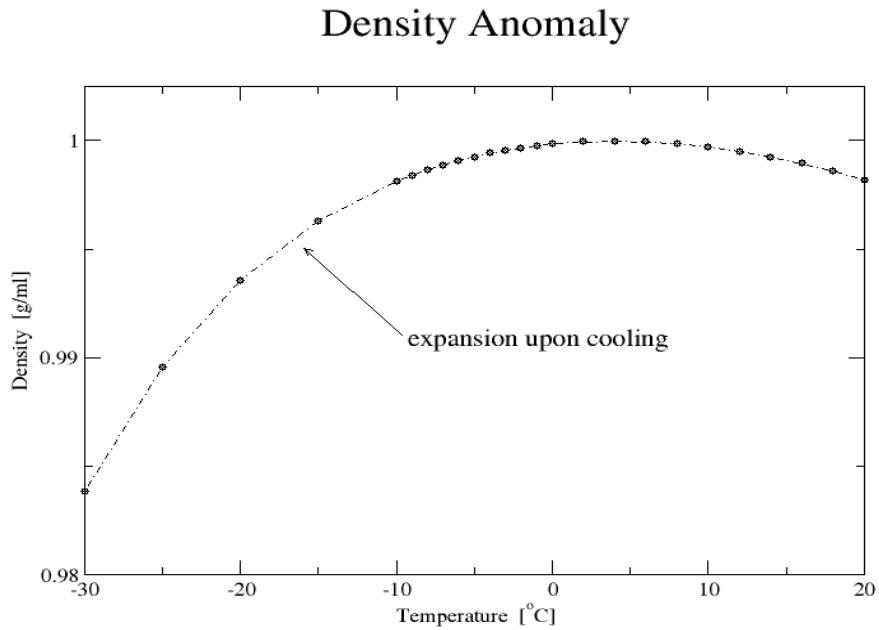


# Liquid water has some unusual properties



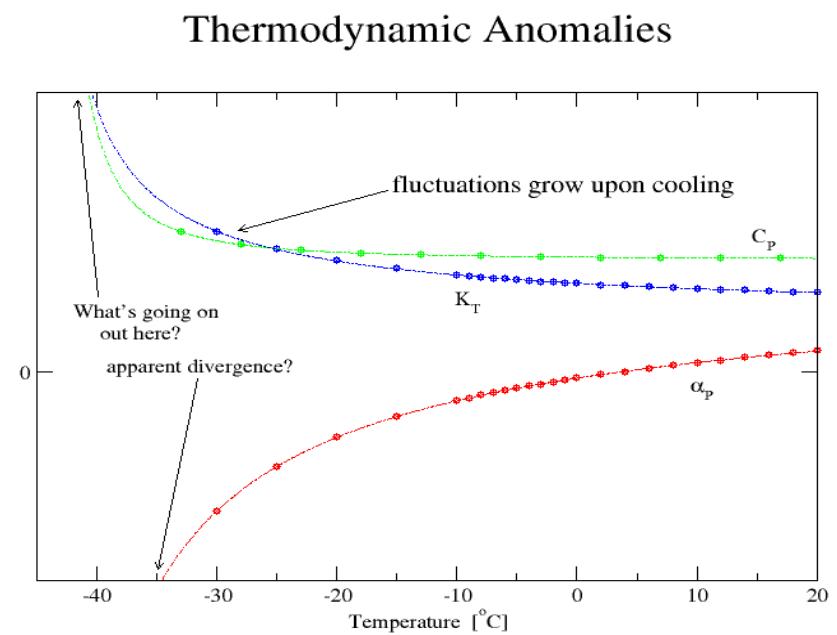
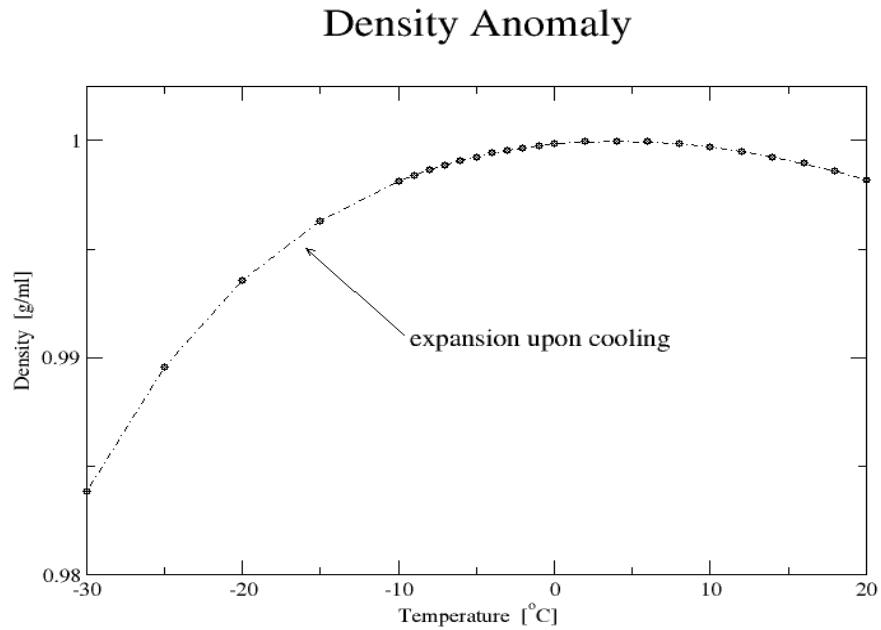
Data from Kell, except  $C_p$  from Angell et al. Lines for  $C_p$ ,  $K_T$ , and  $a_p$  are power law fits.

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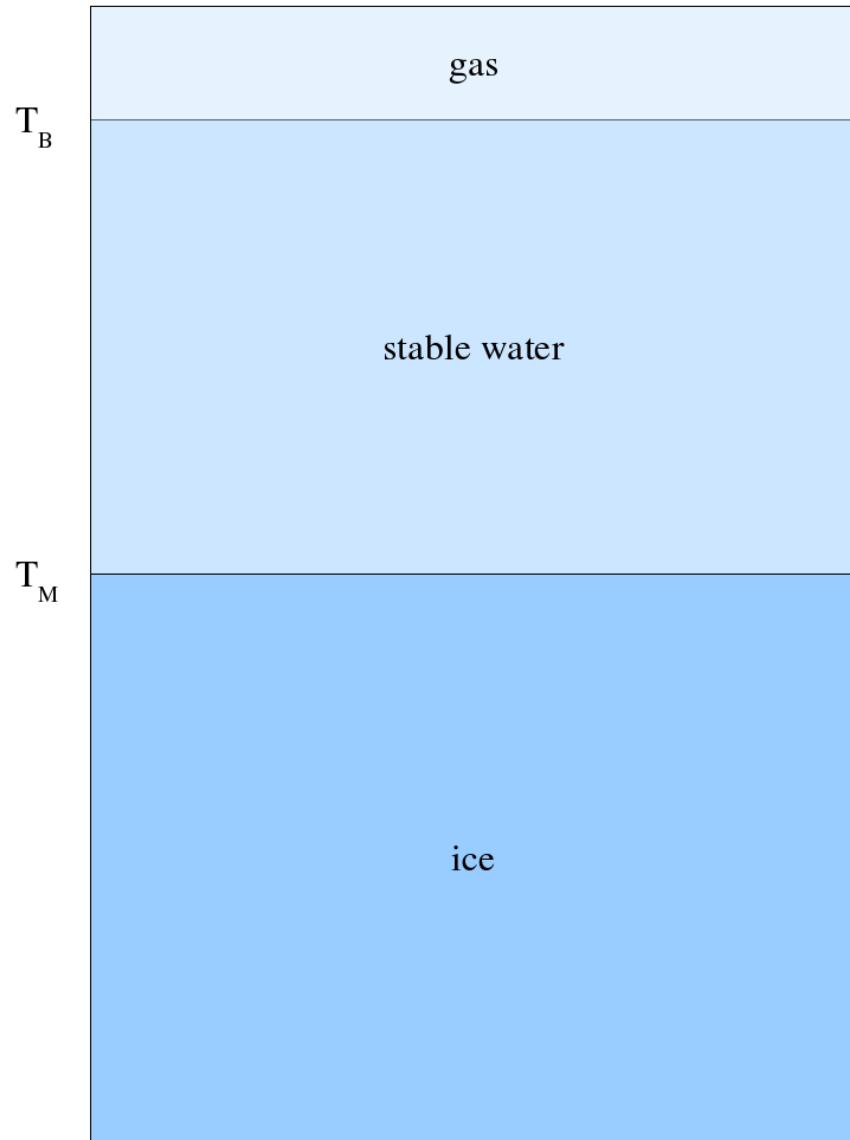
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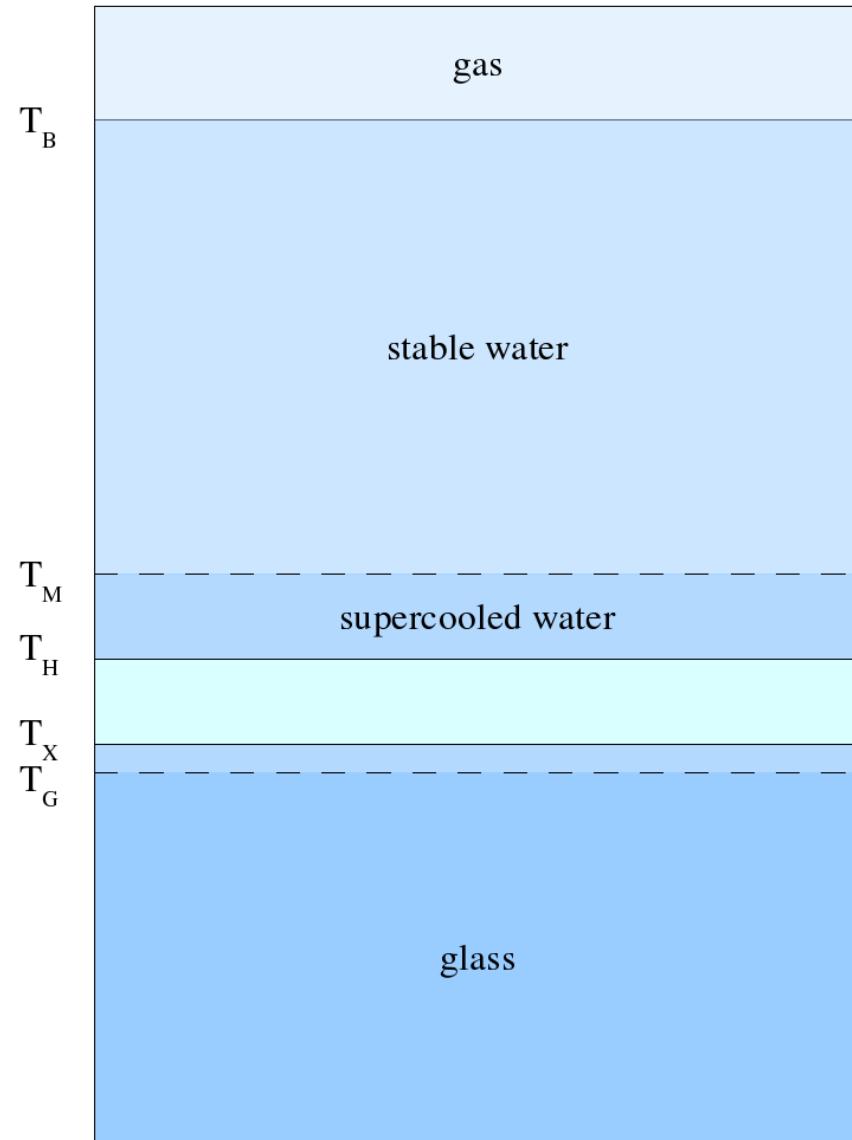


It would be nice to know the phase diagram.

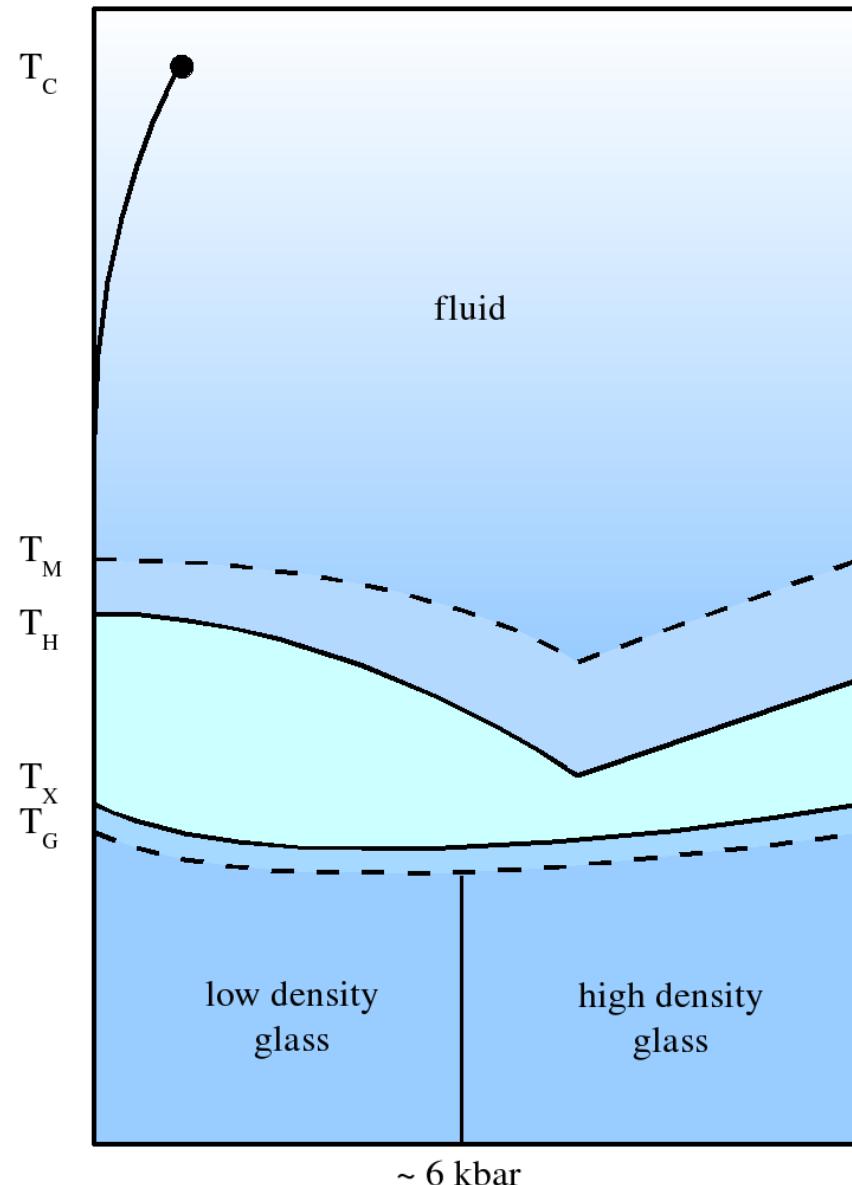
# The phase diagram of water

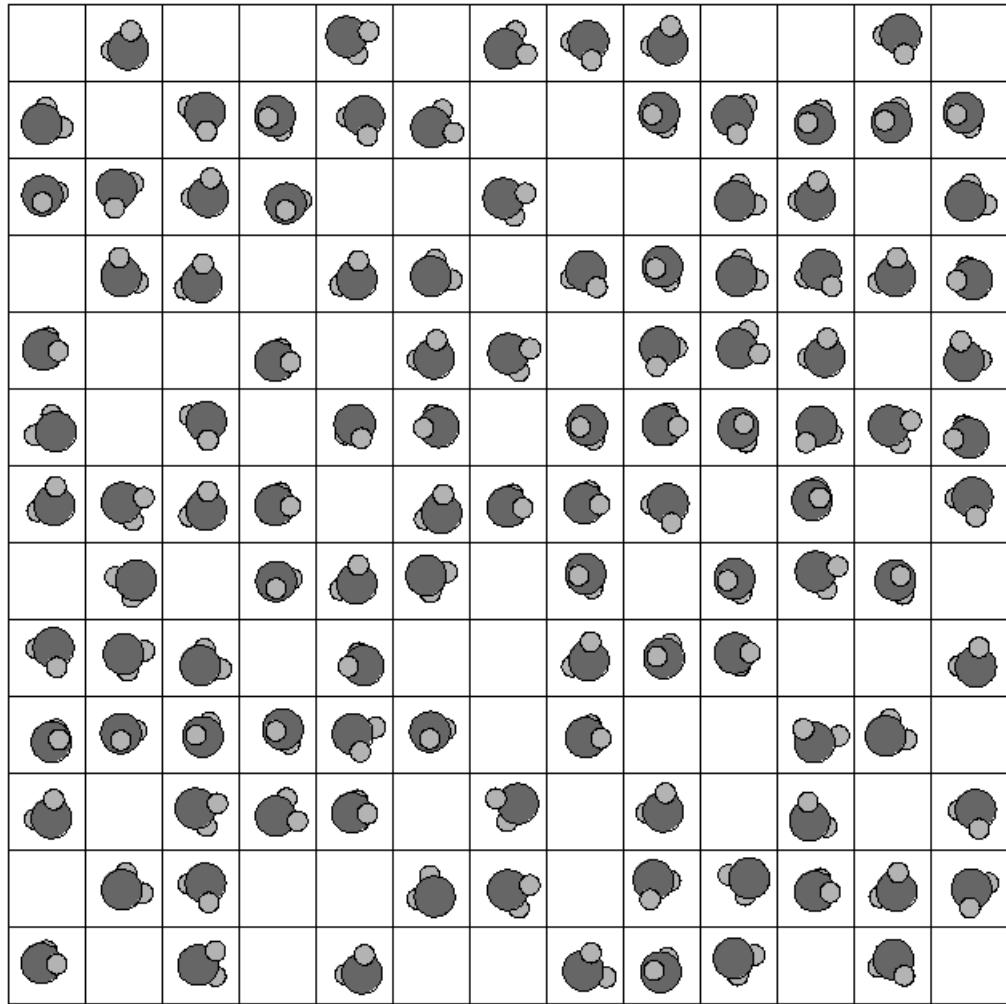


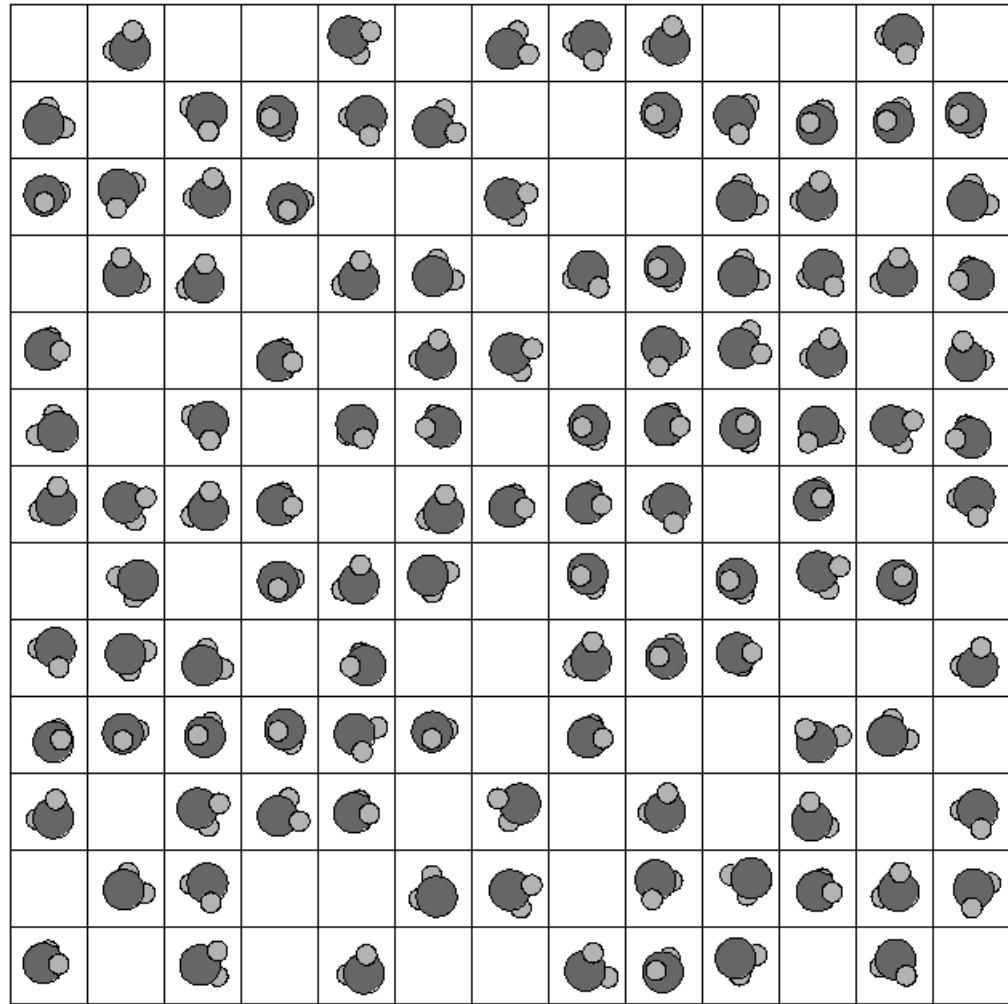
# The phase diagram of fluid water



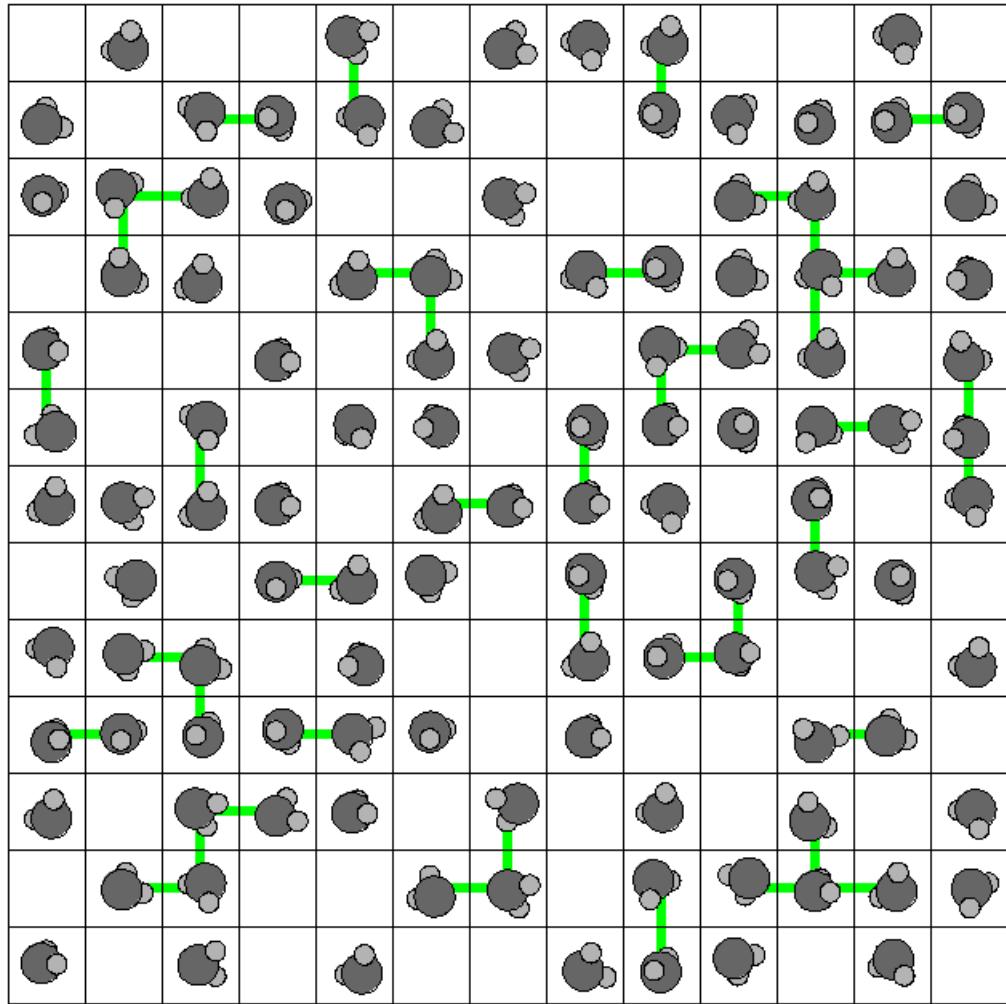
# The phase diagram of fluid water



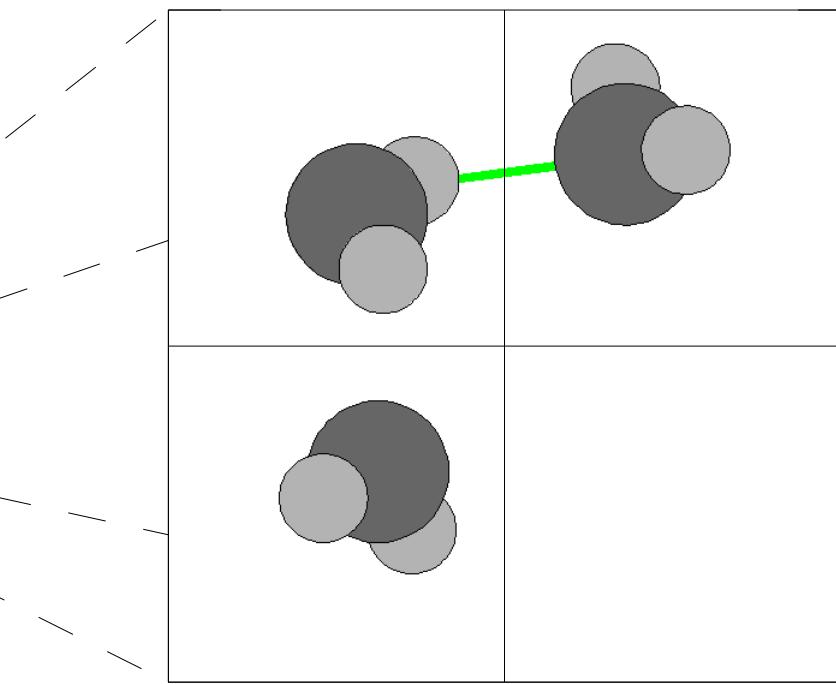
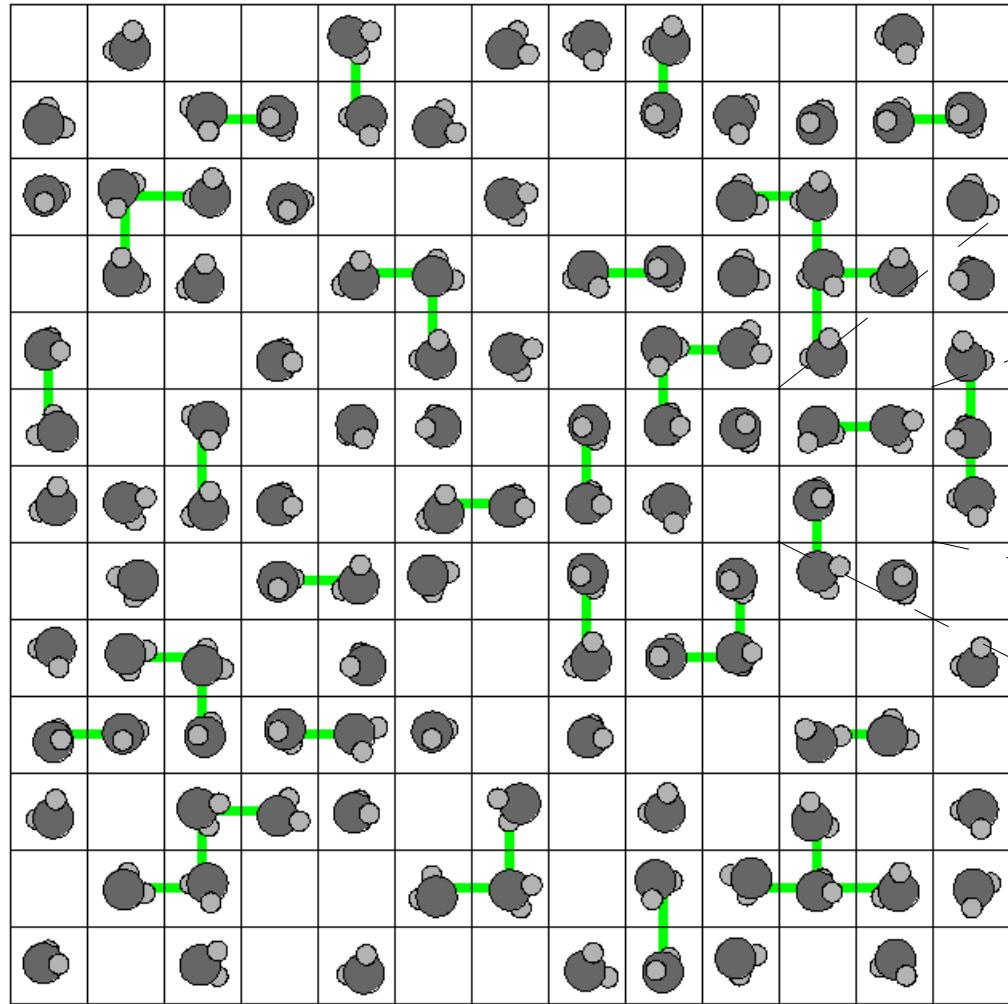




Model = Lattice Gas

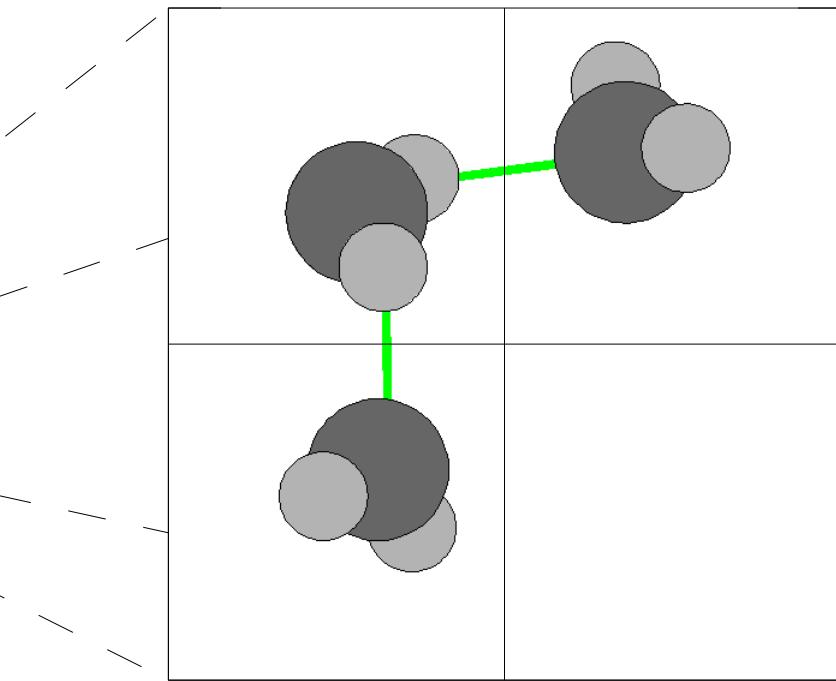
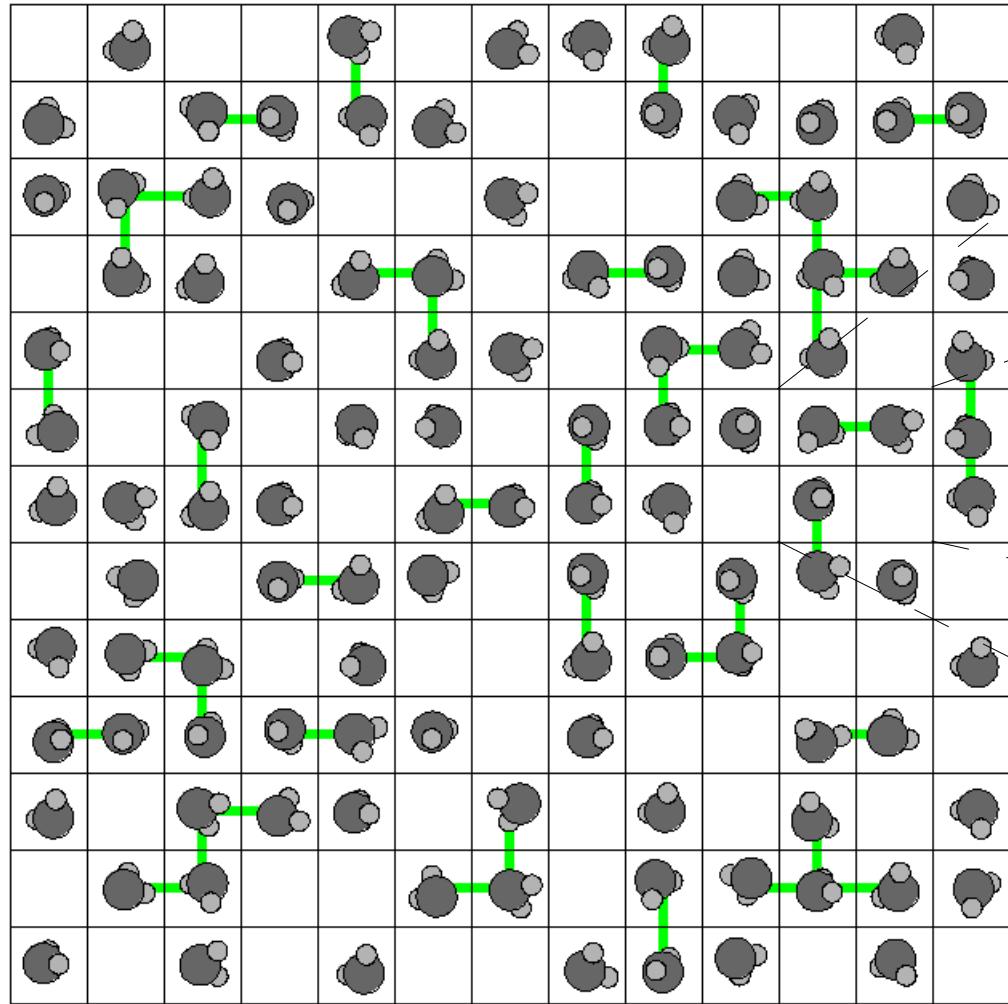


Model = Lattice Gas + Hydrogen Bonds



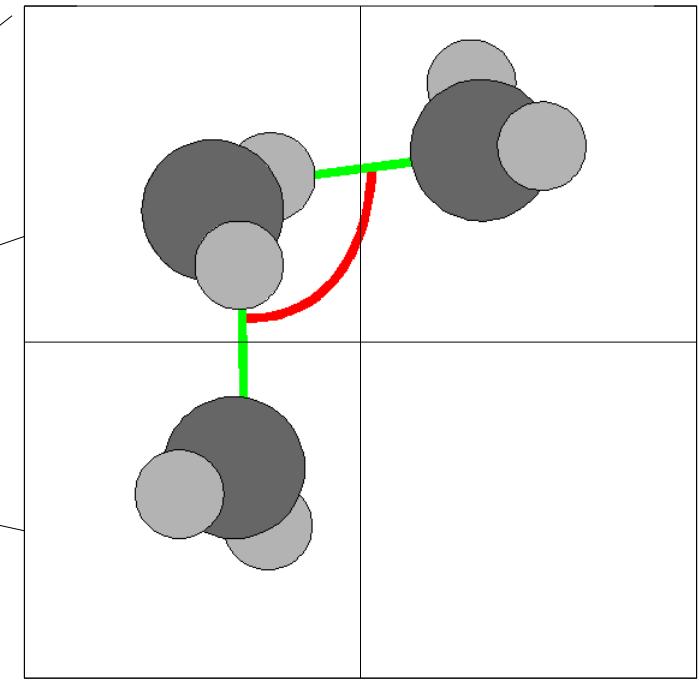
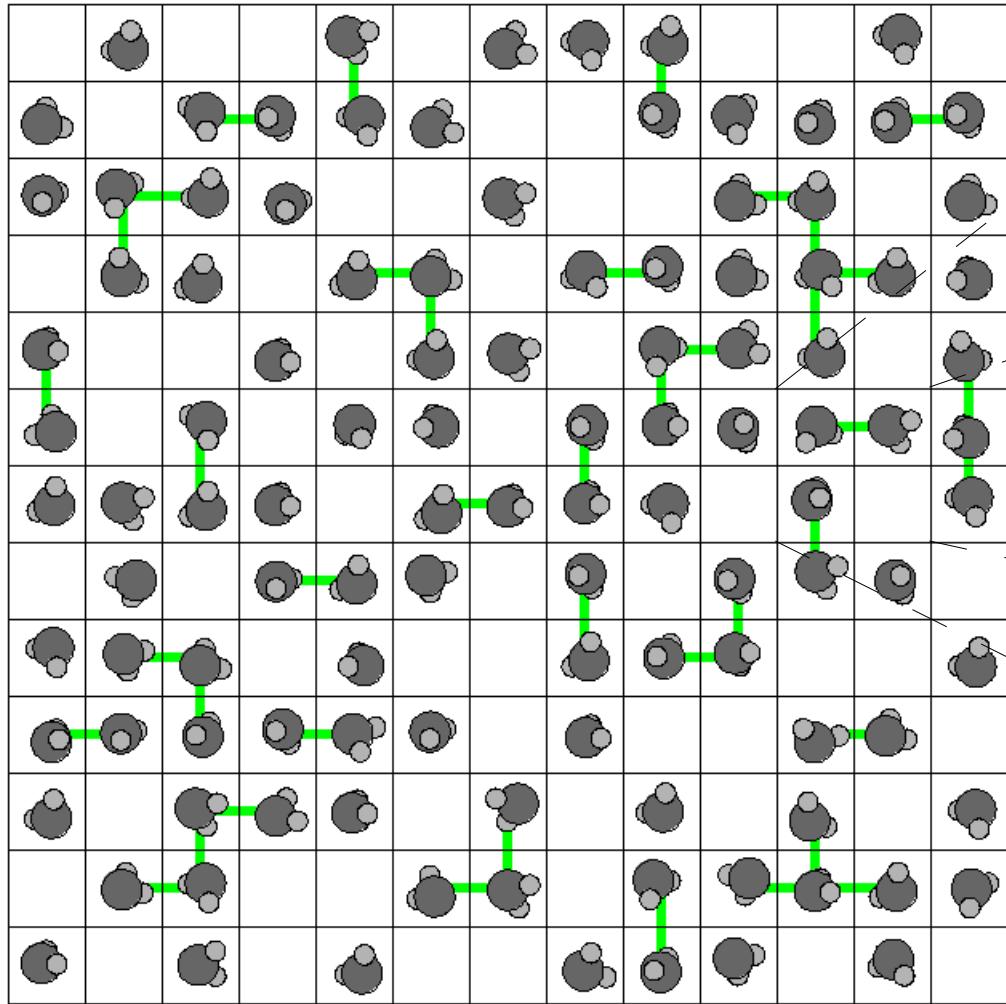
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Pair Energy:  $J$   
Volume Increase



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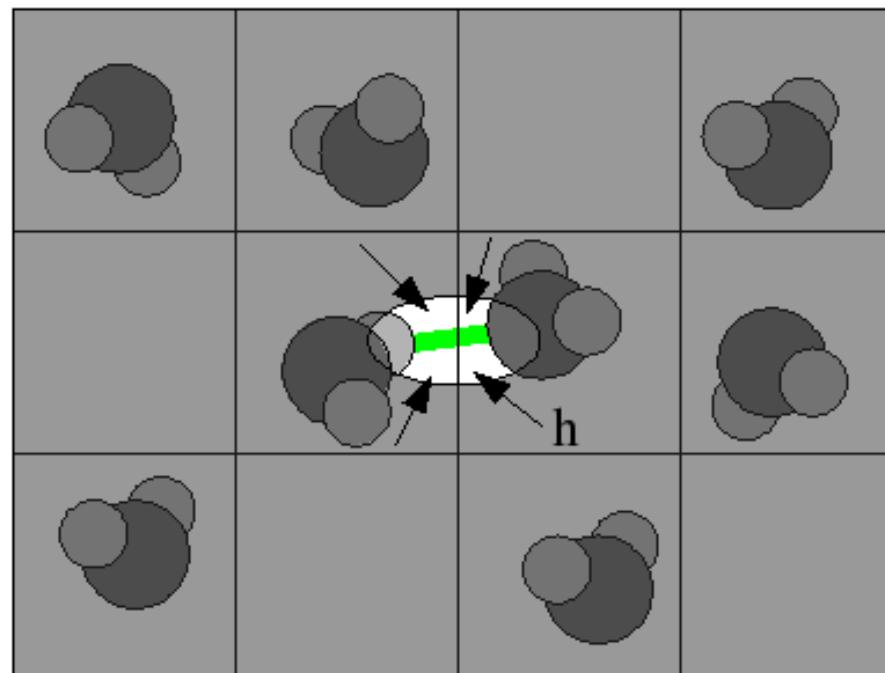


Model = Lattice Gas + Hydrogen Bonds

Pair Energy:  $\mathbf{J}$   
Volume Increase

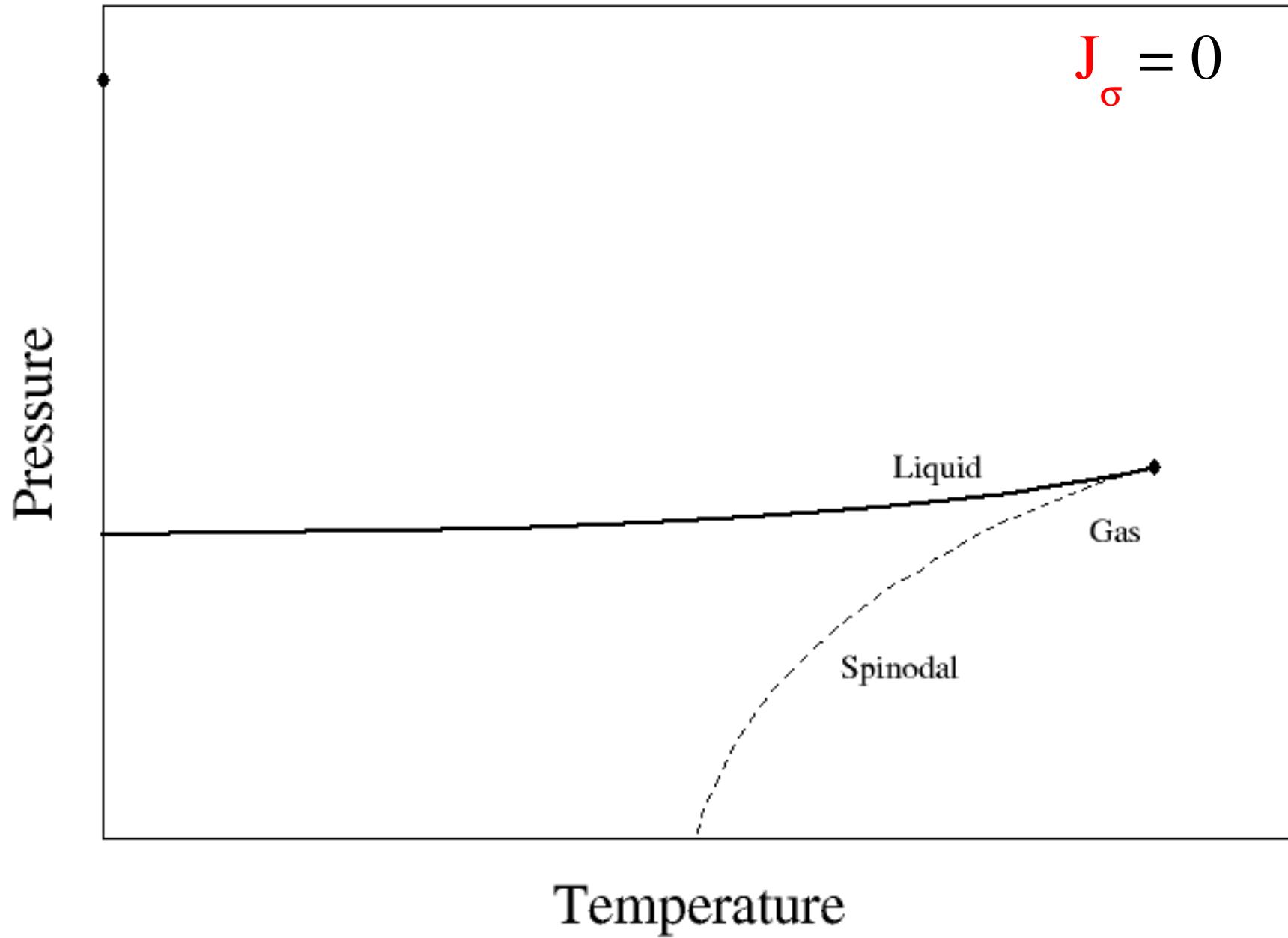
Many-body Energy:  $\mathbf{J}_\sigma$

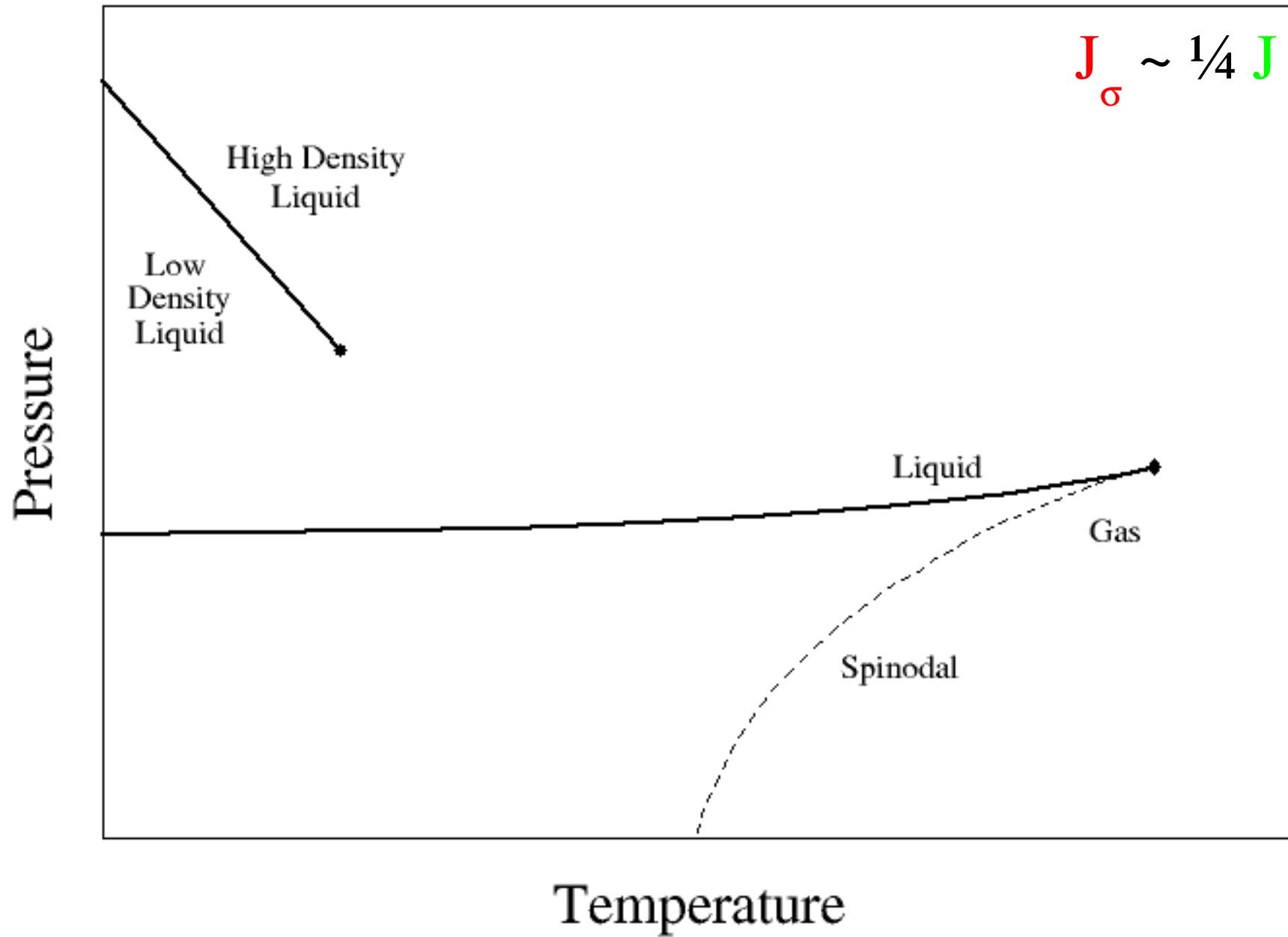
The model may be solved  
within a cavity approximation.

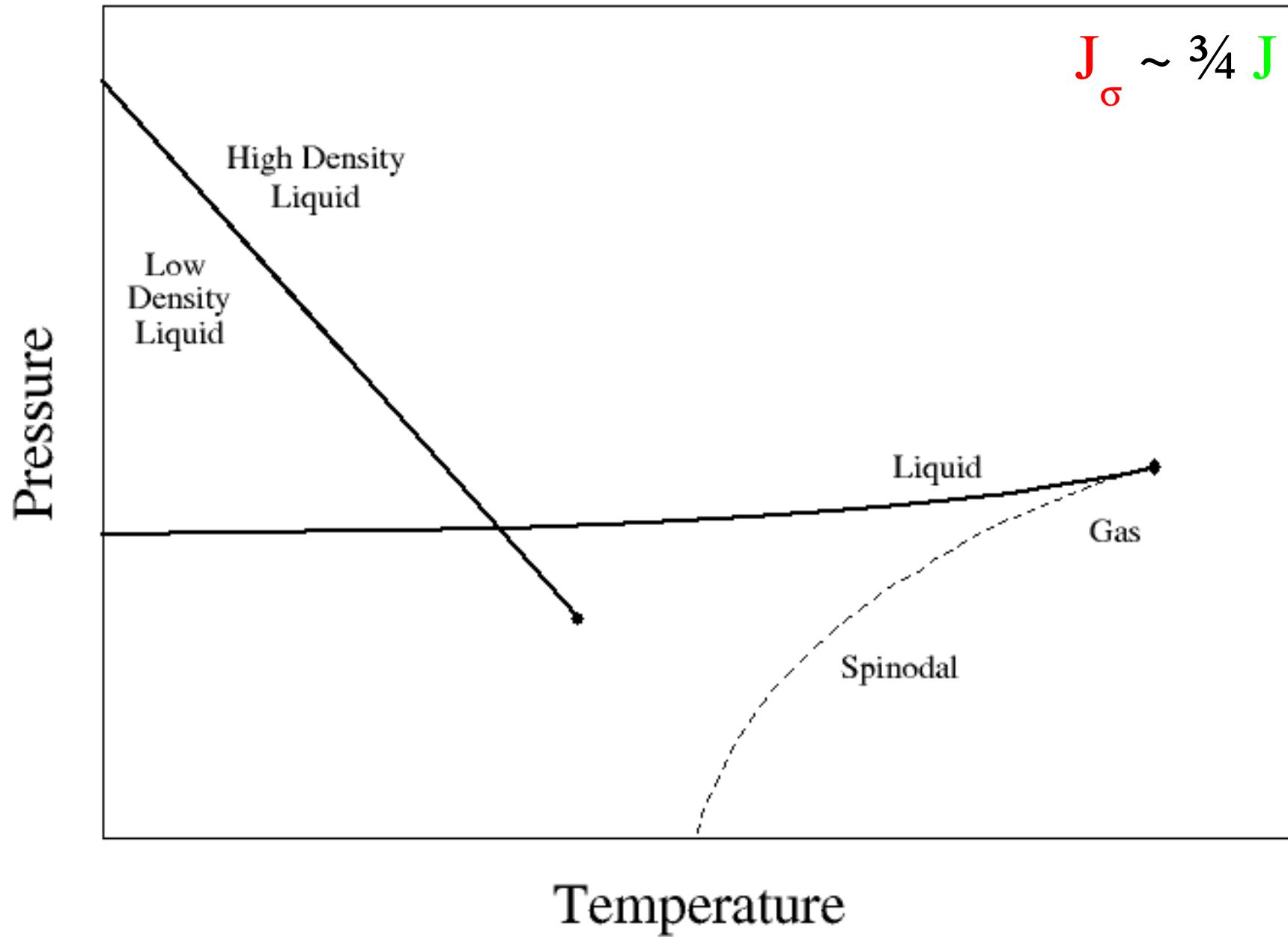


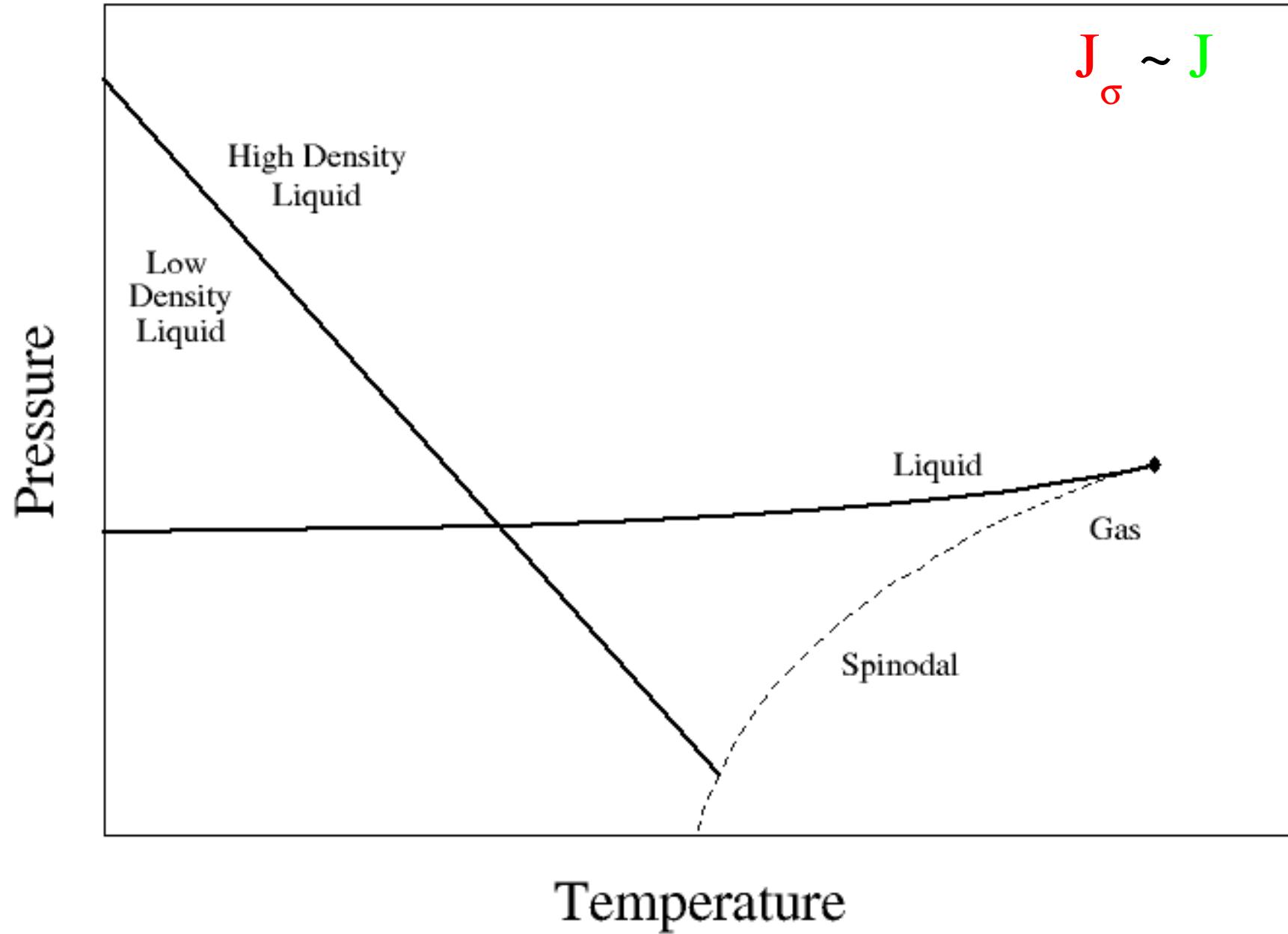
G. Franzese, M. I. Marques, and H. E. Stanley  
"Intramolecular Coupling as a Mechanism for a Liquid-Liquid Phase Transition"  
Phys. Rev. E 67, 011103 (2003)

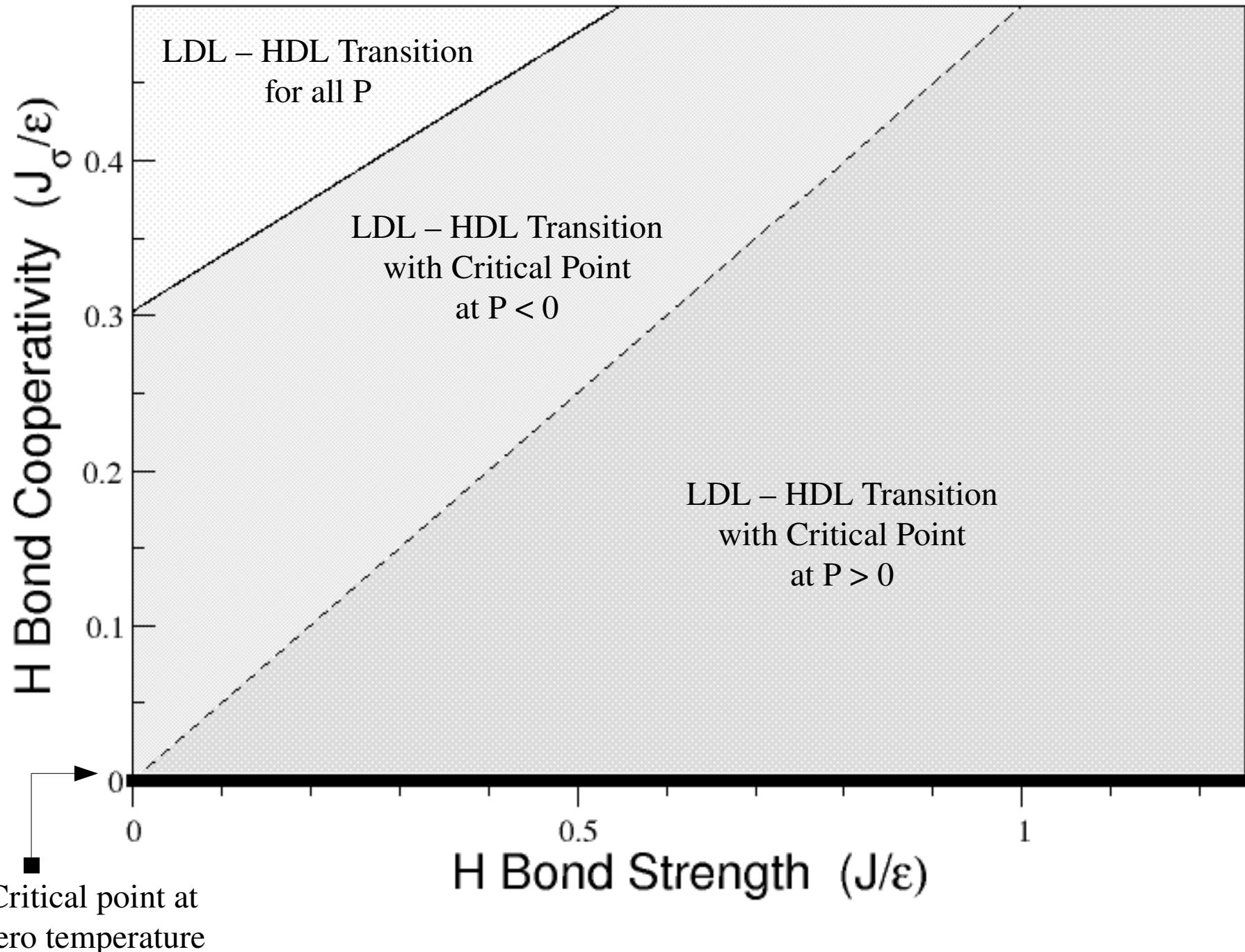
K. Stokely, M. G. Mazza, H. E. Stanley, and G. Franzese  
"Effect of Hydrogen Bond Cooperativity on the Behavior of Water"  
Proc. Natl. Acad. Sci. USA 107, 1301 (2010)











# Take Home Message:

Model = Lattice Gas + Hydrogen Bonds

Several low temperature phase behaviors arise,  
depending on the relative strength of the  
pair and many-body H bond energies.

K. Stokely, M. G. Mazza, H. E. Stanley, and G. Franzese  
Proc. Natl. Acad. Sci. USA 107, 1301 (2011).



